3 Section D b) · Reflexivity: Let (a, b) be an arbitrary element belonging to NXN So, (a, b) E NXN $As, \quad a - a = b - b = 0,$ (a, b) R (a, b) for all $(a, b) \in N \times N$ · R is suffexive Symmetric: Let (a,b), (E,d) E N×N such that (a,b) R (c,d). So. a-c=b-d [Given Relation] Multiplying by (-1) on both sides, $\mathcal{L} - \mathbf{a} = \mathbf{a} - \mathbf{b}$ Hence, (c,d) R (a,b) For (a, b) R (c, d) there is (c, d) R (a, b) for (a, b), (c, d) ENXN

: Ris symmetric · Transitivity: Let (a, b), (c, d), (e, f) E NXN such that (a, b) R (c, d) and (c,d) R (e, F) From the two orelations, a-c=b-d c-e=d-F -2 (1) + (2)a - c + c - e = b - d + d - kSo, $a - e = b - \beta$ Hence, $(a, b) \in Ce, F$ For (a,b) R(c,d) and (c,d) R(e,F) ⇒ (a,b) R(e,F) for (a,b), (c (e, F) E NXN Hence, R is transitive As R is suffexive, Symmetric and transitive, hence R is equivalence scelation.

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As the required line bisects line segment AB, midpoint of line segment AB lies on sequired line. Let midpoint of line segment AB be P. $P = \left(\begin{array}{c} 2+4 \\ 3+5 \\ -2 \end{array}\right) \left(\begin{array}{c} 4+8 \\ -2 \end{array}\right) = \left(\begin{array}{c} 3, 4, 6 \end{array}\right)$ As required line is perpendicular to two lines, $L_1: \frac{x-8}{3} = \frac{y+19}{-16} = \frac{z-10}{7} \text{ and } L_2: \frac{x-15}{3} = \frac{y-29}{8} = \frac{z-5}{-5}$ the direction vector of required line is found by taking cross product of direction vectors of ' and L2. Lot direction vector of required line by be a $\vec{a} = (3\hat{\iota} - 16\hat{\iota} + 7\hat{k}) \times (3\hat{\iota} + 8\hat{\iota} - 5\hat{k})$ - 5 $= \hat{i} (80 - 56) - \hat{j} (-15 - 21) + \hat{k} (24 + 48)$ $= 24\hat{i} + 36\hat{j} + 72\hat{k}$

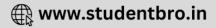
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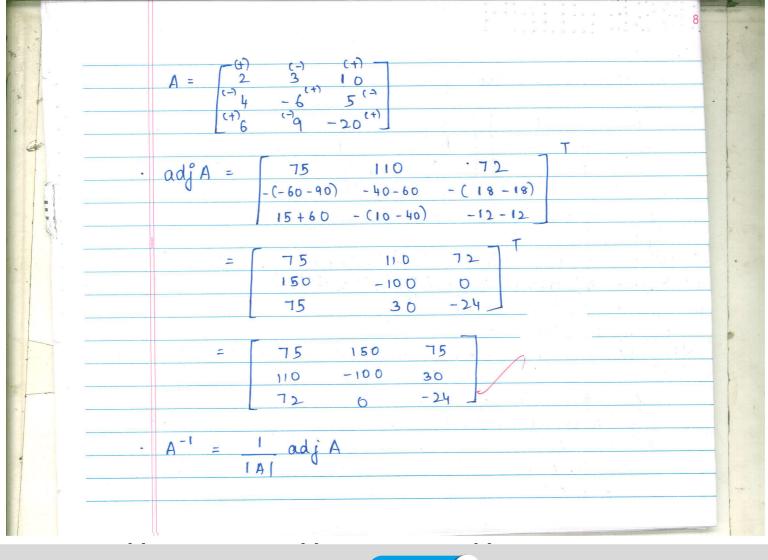
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DR's of sugained line = $\langle 24, 36, 75\rangle = \langle 2, 3, 6\rangle$ Simplified Direction vector = $27 \pm 3\hat{j} \pm 6\hat{k}$ So, Required line is $\vec{R} = \vec{OP} + \lambda(2\hat{i}+3\hat{j}+6\hat{k})$ $\vec{x} = 3\hat{\imath} + 4\hat{j} + 6\hat{k} + A(2\hat{\imath} + 3\hat{j} + 6\hat{k})$ [Vector equation] Cartesian equation: x - 3 = y - 4 = z - 634)(a) let 1 = a, 1 = b, 1 = c. The equations are, 2a + 3b + 10c = 44a - 6b + 5c = 16a + 9b - 20c = 2

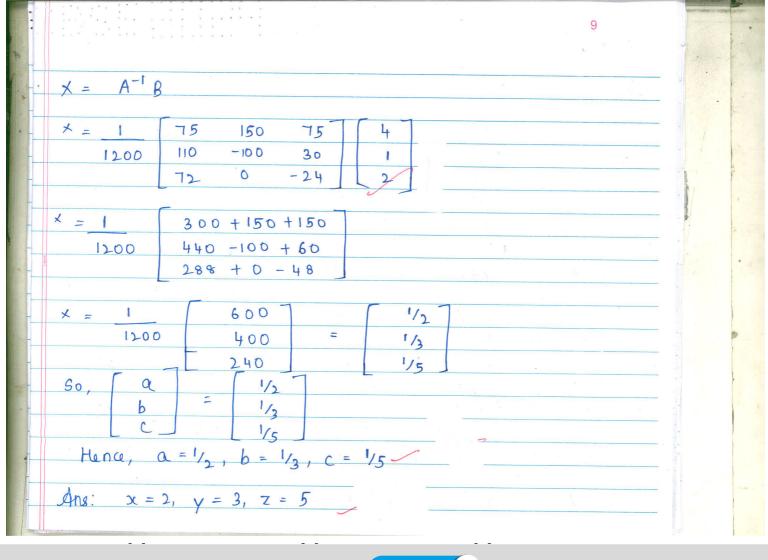
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$$\begin{array}{c} x = 1 \\ x = 4 \\ \hline x = 4 \\ \hline x = 4 \\ \hline y^{2} = 4x \\ \hline y^{2}$$

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11 Section E $F = V^2$ V + 1 14 500 When V = 40 km/br, $(40)^2 - 40 + 14$ F = 500 4 - 10 + 14 1600 = 500 3.2+4 = = 7.2 (l/100km Ans: F = 7.2 (l/100 km)

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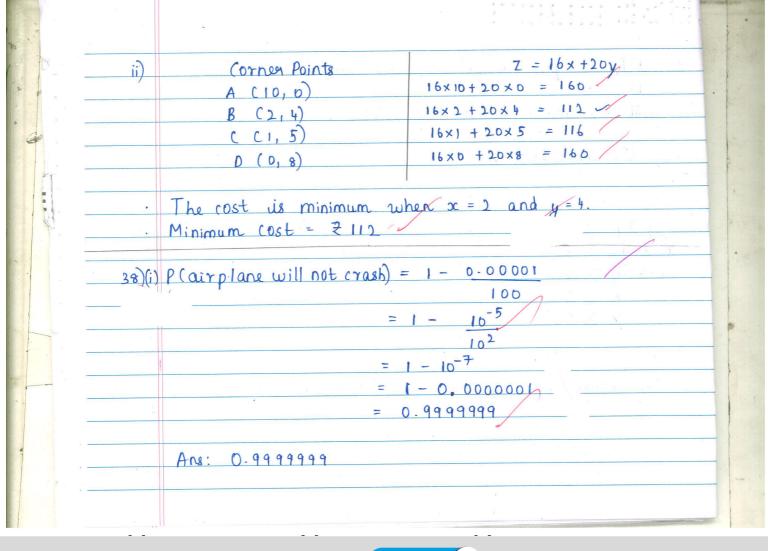
(ii) V² F = - V + 14 500 4 dF 2V1 +0dV 500 dF Ans:-V dv 250 iii) (a) d^2F dv2 250 dF Now, put = 0 dv V V = 0 = 7 250 4 250 4 50, V = 62.5 (km/h)

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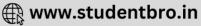
13 As $\frac{d^2 F}{dv^2}$ is positive for v = 62.5 km/hr, Fattains manimum at that point. Ans: V = 62.5 km/hr F $\begin{array}{c} x + 2y > 10 \\ x + y > 6 \\ 3x + y > 8 \end{array}$ i) y >. 0 The above are the constraints determining the feasible region

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15 $P(A/E_1) + P(A/E_2) = 0.95 + 1$ = 1.95 $-ii)aP(A) = P(E_1) \cdot P(A/E_1) + P(E_2) \cdot P(A/E_2)$ $= (10^{-7})(0.95) + (1 - 10^{-7})(1)$ = 0.95×10-7 + + -10-7 = 1 - 0.05 × 10-7 $= 1 - 5 \times 10^{-9}$ 1 - 0.000000050.999999995 Ans: p(A) = 0.999999995

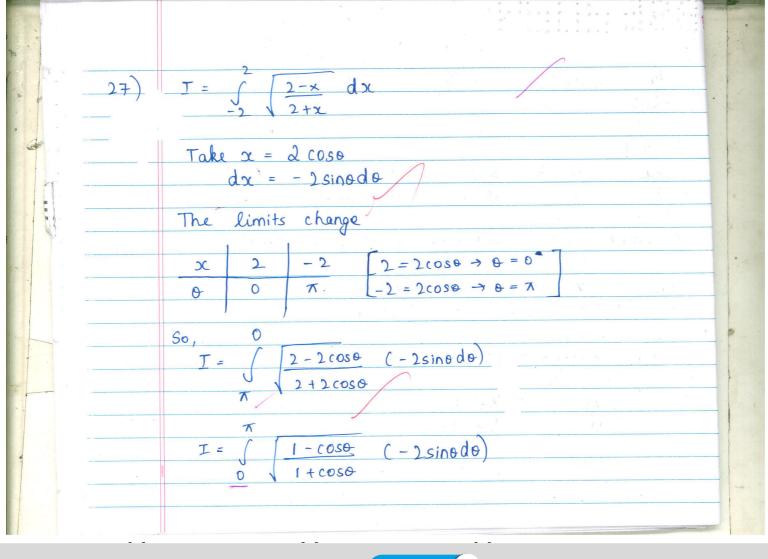
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Section C $26)(a) x = e^{\cos 3t}$ Taking log on both sides, logex = cos 3t - D Differentiating w.r.t t, $\frac{1}{2c} \frac{dx}{dt} = -3sin3t$ $s_0, dx = x(-3sin3t) - 0$ p sin3t Taking log on both sides, log y = sin 3t - 3 Differentiating w.r.t t, 1 dy = 3 cos 3t

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17 = y (3 cos 3t) - (4) (4) ÷ 2 $\frac{dy}{dx} = \frac{y(3\cos 3t)}{x(-3\sin 3t)} = \frac{-y(\cos 3t)}{x(\sin 3t)}$ As log x = cos 3t and logy = sin 3t from () and (), - y logx x logy $\frac{dy}{dx} = \frac{-y}{x} \frac{(\log x)}{(\log y)} - \frac{1}{2}$ Hence proved that dy = - y logx dr x logy



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19 $I = \begin{pmatrix} Z \sin^2 \theta/2 & (-2 \sin \theta d\theta) \\ 2 \cos^2 \theta/2 \end{pmatrix}$ $I = \int tane_{2} (-2sinede)$ Using property $\int \beta(x) dx = -\int \beta(x) dx$ $I = \int (tan \theta_2) (2sined \theta) \int Sin \theta = dsin \theta_2 cos \theta_2$ $T = \sqrt{\frac{\sin\theta_{12}}{\cos\theta_{12}}} \left(\frac{4\sin\theta_{12}}{\cos\theta_{12}} \cos\theta_{12}}\right)$ $I = 4 \int \sin^2 \theta_2 \, d\theta$ $I = 4 \int (1 - \cos \theta) d\theta$

$$T = 2\int_{0}^{\pi} (1 - \cos \theta) d\theta$$

$$= 2\left(\theta - \sin \theta\right) I_{0}$$

$$= 2\left((\pi - \sin \pi) - (0 - \sin \theta)\right)$$

$$= 2\pi$$

$$28)(\theta) 2xy + y^{2} - 2x^{2} dy = 0.$$

$$dx$$

$$dy = 2xy + y^{2}$$

$$dx = 2x^{2}$$

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Sub
$$y = V$$
 in (1) and equate (1) and (2)
 $x = V + 1 = V^2$
 $dx = V^2$
 $dx = 2$
So, On $re - arranging_1$
 $\int dx = 2 \int dV$
Integrating on both sidu,
 $ln [x] + c = 2 \int V^{-2} dV$
 $ln [x] + c = 2 \int V^{-2} dV$
 $ln [x] + c = 2 \int V^{-2} dV$

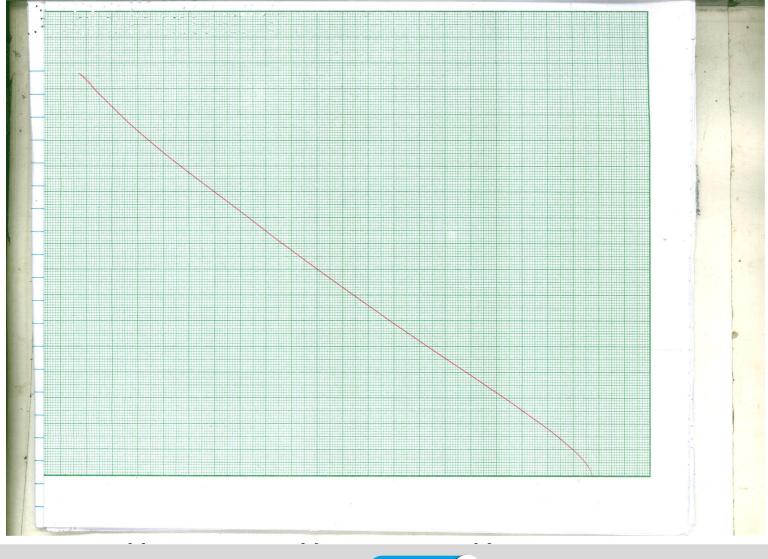
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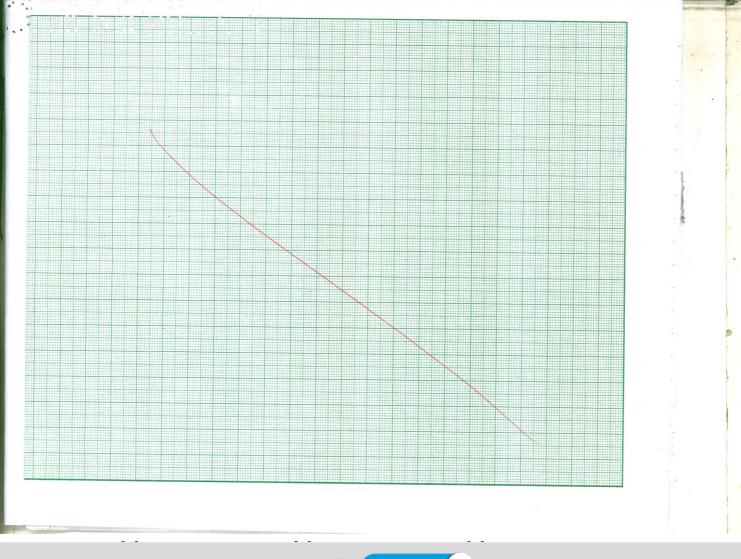
ln|x|+c = -2 = -2x [V = 4] so, c = -2x - ln(x)Griven: $y(\hat{I}) = 2$ $S_{0}, C = -2(1) - ln(1)$ C = -1 Particular solution is, ln|x| - 1 = -2x $\frac{y}{y = -2x} = 2x$ lo(x) - 1 1 - lo(x)Ans: y = 2x1 - ln[x]

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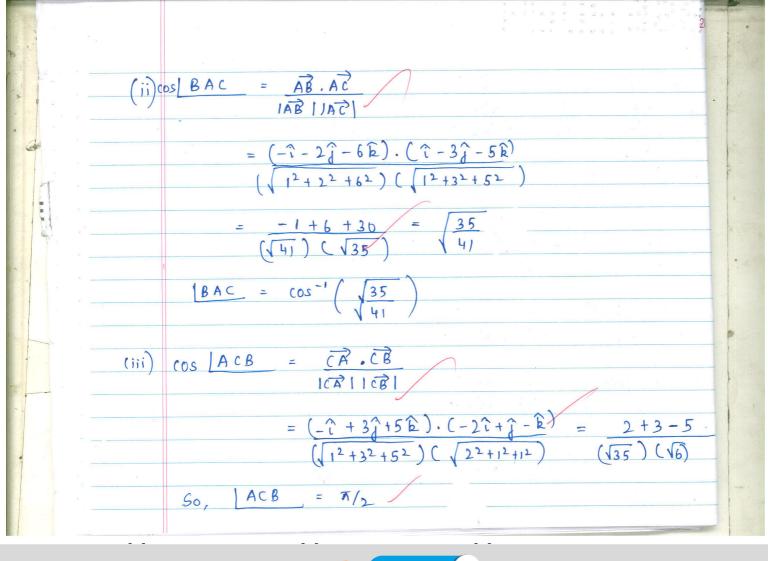


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27 3) $\begin{array}{rcl} & \overrightarrow{OA} &=& 2\hat{\iota} - \hat{\jmath} + \hat{\Bbbk} \\ & \overrightarrow{OB} &=& \hat{\imath} - 3\hat{\jmath} - 5\hat{\Bbbk} \\ & \overrightarrow{OZ} &=& 3\hat{\iota} - 4\hat{\jmath} - 4\hat{\Bbbk} \end{array}$ $\cdot \overrightarrow{AB} = \overrightarrow{OB} - \overrightarrow{OA}$ $= -\hat{i} - 2\hat{j} - 6\hat{k}$ $\vec{BC} = \vec{OC} - \vec{OB}$ $= 2\hat{i} - \hat{j} + \hat{k}$ \cdot $(\overrightarrow{A}) = (\overrightarrow{A}) - (\overrightarrow{A})$ $= -\hat{i} + 3\hat{j} + 5\hat{k}$ $\frac{\cos \left[ABC\right]}{\left[B\overline{A}\right]} = \frac{B\overline{A}}{B\overline{A}} \cdot \frac{B\overline{C}}{B\overline{C}}$ $(\hat{\iota}+2\hat{j}+6\hat{k}).(2\hat{\iota}-\hat{j}+\hat{k})$ (i) $(\sqrt{1^2+2^2+6^2})(\sqrt{2^2+1^2+1^2})$ 2-2+6 6 41) (16) S_{0} | ABC = $\cos^{-1} \int \sqrt{6/41}$

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29 Ans: $BAC = cos^{-1} \sqrt{35}$, $ABC = cos^{-1} \sqrt{6}$, $ACB = \pi/2$ 30) Let X denote the absolute difference of numbers appearing on top of dice x can take values 0, 1, 2, 3, 4, 5. • For $x = 0 \rightarrow \{ (1, 1), (2, 2), (3, 3), (4, 4), (5, 5), (6, 6) \}$ P(x = 0) = 6 = 136 6 For $x = 1 \rightarrow \{(1, 2), (2, 3), (3, 4), (4, 5), (5, 6), (2, 1), (3, 2), (4, 3), (5, 4), (5, 6),$ (6,5)? 5 P(x=i) = 10 = 536 18 =0

• For $x = 2 \rightarrow \{(1, 3), (2, 4), (2, 5), (4, 6), (3, 1), (4, 2), (5, 3), (6, 4)\}$ 4p(x=2) = 8 = 2For $x = 3 \rightarrow \{(1, 4), (2, 5), (3, 6), (4, 1), (5, 2), (6, 3)\}$ $4p(x=3) = \frac{6}{34} \neq 1$ For x = 4 > { (1,5), (2,6), (5,1), (6,2)} 1 p(x = 4) = 4 = 136 9 - For $x = 5 \rightarrow \{(1,6), (6,1)\}$ $4 p(x=\hat{s}) = 2 = \frac{1}{18}$

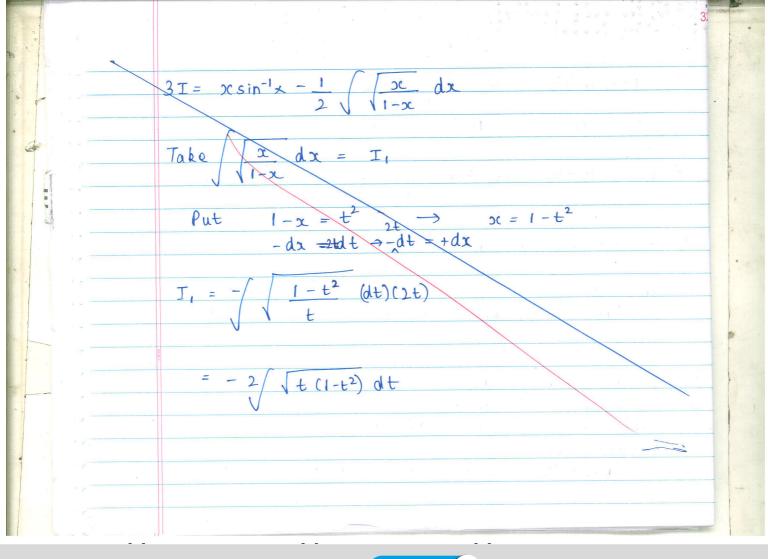
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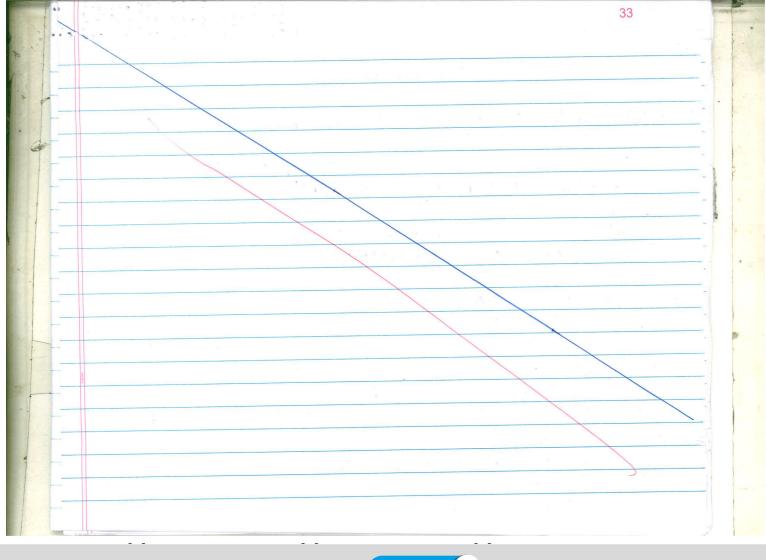
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31 The Probability distribution table is, 0 30 2 3 4 5 $P(x) = \frac{1}{6} = \frac{6}{36} = \frac{10}{36} = \frac{51}{18} = \frac{8}{36} = \frac{21}{9} = \frac{6}{36} = \frac{1}{6} = \frac{1}{9} = \frac{21}{35} = \frac{1}{18}$ 3) $T = \sqrt{x^2 \cdot \sin^{-1}(x^{3/2})} dx$ Take it = x2 $dt = 3x^2 dx \rightarrow dt = x^2 dx$ Jx = t So, $J = \frac{1}{2} (i) \sin^{-1} (\sqrt{x}) dx$ $\frac{1}{2\sqrt{2}} dx = dt \quad dx = 2tdt$ Take $U = \sin^{-1}(\sqrt{x})$, dV = dxApplying By - Parts, 2sin-t- ft2 dt $3I = x \sin^{-1} x - \left(x \left(-\frac{1}{2} \right) \cdot \left(\frac{1}{2} \right) dx \right)$ [1-+2 VI - 2C 212

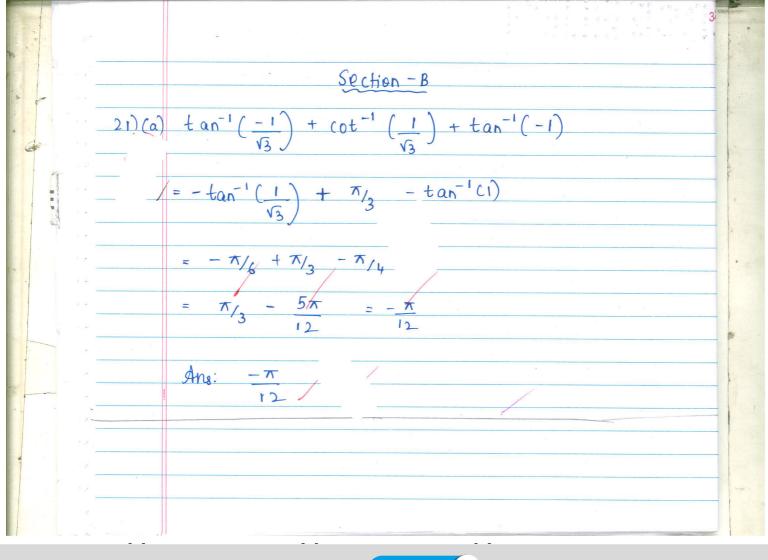
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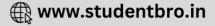
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35))) y = cosec (cot'x)dy = - cosec (cot x). (ot (cot x). (-1) - x cosec (tot-'x) $\int coseco = \sqrt{1+cot^{2}\theta}$ = 1 + cot2 (cot-'x) $-\chi \sqrt{1+\chi^2}$ = $y = (Osec (iot^{-1}x))$ Diff wr.t.x,2))) $\frac{dy}{dx} = -\cos ec(\cot^{-1}x) \cdot \cot c \cot^{-1}x) \cdot \left[\frac{r}{1+x^2} \right] \quad [\cot(\cot^{-1}x) = x]$ dy = x cosec (cot-x) COSELO = (1+cot20 de 1+x2

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x $1 + \cot^2 (\cot^{-1}x)$ dy dr $1+x^2$ $\chi(\sqrt{1+\chi^2})$ dy = dx +x2 dy X dx V1+x2 So, $(\sqrt{1+x^2}) dy = x$ dx $\left(\sqrt{1+x^{2}}\right) \frac{dy}{dx} - x = 0.$ Hence, Proved the required .

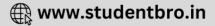
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37 13, = x + 1oc Diff wrt x on both sides $f'(\mathbf{x}) =$ x 2 Put f'(x) = 0 $1 - \frac{1}{x^2} = 0 \Rightarrow 1 = 1 \Rightarrow x^2 = 1$ x^2 So, $x = \pm 1$ Now, f''(x) = 2 x^3 = 2 70 attains minima at x = 1. ACX

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f''(-1) = 2 < 0 $\beta(x)$ attains maxima at x = -1. So, M = , m=/ M-m = · Local maximum value = M = F(-1) = -1 + 1 = -2· Local minimum value = m = f(i) = 1 + 1 = 2So, M - m = -2 - (2)Ans: - 4





39 $T = \left(\frac{e^{4x}-1}{e^{4x}+1}\right) dx$ Divide Numerator and Denominator by duy e²² 50, $I = \frac{(e^{2x} - e^{-2x}) dx}{e^{2x} + e^{-2x}}$ Take $U = e^{2x} + e^{-2x}$ $dv = (2e^{2x} - 2e^{-2x})dx$ $S_0, \ dv = (e^{2x} - e^{-2x}) dx$ Hence, $I = \frac{1}{2} \left(\frac{dU}{U} = \frac{1}{2} \log_{e} |U| + C \right)$ Ans: $T = \frac{1}{2} \log \left[\frac{1}{e^{2x}} + e^{-2x} \right] + C$

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25)
$$f(x) = e^{+x} - e^{-x} + x - tan^{-1}x$$

Different lating w.r.t x,
 $f'(x) = e^{x} + e^{-x} + 1 - \frac{1}{1+x^{2}}$
 $= e^{x} + e^{-x} + \frac{1+x^{2}-1}{1+x^{2}}$
 $= e^{x} + e^{-x} + \frac{1+x^{2}-1}{1+x^{2}}$
 $= e^{x} + e^{-x} + \frac{1+x^{2}}{x^{2}}$
For any value of x in its damain,
 $e^{x} > 0$, $e^{-x} > 0$, $\frac{x^{2}}{x^{2}} > 0$ $\left[\frac{-1}{1+x^{2}} + \frac{1-1-1}{1+x^{2}} + \frac{1+x^{2}}{1+x^{2}} + \frac$

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41 As f'(x) is always greater than 0, f(x) is a strictly increasing function Section - A Product = D Ans: (A) D $\frac{1}{2} f(x) = 9x^2 + 6x - 5$ $= (3x)^2 + 2(3x)(1) + 1 - 6$ $= (3x+1)^2 - 6$ $= (3x+i)^2 - 6$ Griven: x>0 32 >0 $3x+1>_1 \rightarrow (3x+1)^2>_1$ S_0 $(3x+1)^2 - 6 > -5$ Ans: (c) Bijective

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3)
$$\begin{vmatrix} -a & b & c \\ a & -b & c \\ a & -b & c \\ \end{vmatrix} = abc \begin{vmatrix} -1(1-b) - 1(b) - 1(b) \\ 1 & 1 & -1 \\ \end{vmatrix}$$

= $abc \begin{bmatrix} -1(1-b) - 1(b) - 1(b) + 1(b) \\ 1 & 1 & -1 \\ \end{vmatrix}$
= $abc \begin{bmatrix} 2+2 \\ 2+2 \\ 2+2 \\ 2+2 \\ \end{vmatrix}$
= $4abc = babc \begin{bmatrix} b = 4 \\ 2+2 \\ 2+2 \\ 2+2 \\ \end{vmatrix}$
= $4abc = babc \begin{bmatrix} b = 4 \\ 2+2 \\ 2+2 \\ 2+2 \\ 2+2 \\ \end{vmatrix}$
= $4abc = babc \begin{bmatrix} b = 4 \\ 2+2 \\ 2+$

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43 $f(x) = x^3 - 3x^2 + 12x - 18$ $\int (x) = 3x^2 - 6x + 12$ = 3 (x² - 2 × + 4) $= 3(x-2)^{2}$ Ans: (B) Strictly increasing on R T/2 T/2 Sinx-cosx dx = (COSX-SINX dx 1+ SINX COSX 1+ SIGXCOSX Ans: (B) Zeroco (A) COSX - Sin (4. (0) 2. 5 < 12/15/ 8) $(\hat{D})(0,0,0)$

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10, (D) a feasible region 1) $P(S/E) = P(S \cap E) = P(E) =$ $P(E) \qquad P(E) \qquad P(E)$ $12) \cdot q_{11} = 1 - 3 = -2$ • $a_{12} = 1 - 6 = -5$, $a_{21} = 2 - 3 = -1$ $S_0, q_1, + q_2 = -6$ $-a_{13} = 1 - 9 = -8$, $a_{31} = 3 - 3 = 0$ Ans: (C) 913> azz $\frac{d(tap^{-1}(x^2)) = 1}{dx} = \frac{1}{1+x^4} = \frac{2x}{1+x^4}$ dac Ans: (B) 2x

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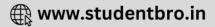
45 44 $\left(\frac{d^2y}{dx^2}\right)^2 + \left(\frac{dy}{dx}\right)^3 = x \sin\left(\frac{dy}{dx}\right)$ Ans: (D) not defined $(\hat{i} + \hat{k}) \times (\hat{i} - \hat{k}) = \hat{j} + \hat{j} = 2\hat{j}$ [Unit vector = \hat{j}] -Ans: (B) j $\frac{x-1}{2} = \frac{y}{-1} = \frac{z+1}{2}$ Ans: (D) 2, -1, 3 $\frac{1}{F(x)^2} = \frac{\cos x - \sin x}{\sin x \cos x}$ (OSK - SIDX O) = (COS2X - SID2X)0 0 COSX 0 Sin2x COS2x 0 0 SINX D b 0 D 0 0 Ang: (B) 2

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18)
$$\chi = 30^{\circ}, \beta = 12.0^{\circ}$$

 $(0s^{2} \chi + (0s^{2} \beta + (0s^{2} \chi = 1))^{2} + (-1)^{2} + (0s^{2} \chi)^{2}$
 $(0s^{2} 30 + (0s^{2} 100 + (0s^{2} \chi) = (\frac{13}{2})^{2} + (-1)^{2} + (0s^{2} \chi)^{2}$
 $= 1 + (0s^{2} \chi)^{2}$
 $50, \ (0s \chi = 0 \Rightarrow \chi_{1} = 90^{\circ}$
 $4ns: (A) 90^{\circ}$
19) $(B'AB)^{T} = B^{T}A^{T}B$
 $= B'AB [CA = A]$
Ans: (D) Assocition (A) is False, but Reason (R) is true
 $-(2b)$ (C) Assocition (A) is true, but Reason (R) is false.





47 $I = (-2^{2} \sin^{-1} (x^{3/2}) dx)$ Let $t^2 = x^3 \rightarrow 2tdt = x^2dx$ So, Sin (Nt) dt $I = \frac{1}{2} \int 2t \sin^2 t \, dt$ Now, dv = 2tdt and $U = sin^{-1}t$ Applying By-parts [UV- NVdu], $3I = t^2 \sin^{-1} t - \int \frac{t^2}{\sqrt{1-t^2}} dt$ $= t^{2} \sin^{-1} t + \int (1 - t^{2} - 1) dt$ = $t^2 \sin^{-1}t + \int (\sqrt{1-t^2})dt - \int dt$

48 $3I = t^{2} \sin^{-1} t + \frac{t}{2} \sqrt{1 - t^{2}} + \frac{1}{2} \sin^{-1} (t) - \sin^{-1} t + c$ $= (t^2 - 1/2) \sin^{-1}t + \frac{t}{t} \sqrt{1-t^2} + C$ Subbing $t^2 = x^3$, E 2024 $3T = (x^{3} - \frac{1}{2}) \sin^{-1}(x^{3/2}) + \frac{x^{3/2}}{2} \sqrt{1 - x^{3} + C}$ So, $I = \frac{1}{3} \left[\left(x^{3} - \frac{1}{2} \right) \operatorname{Sin}^{-1} \left(x^{3/2} \right) + \frac{x^{3/2}}{2} \sqrt{1 - x^{3}} + c' \left[c' = \frac{c}{3} \right] \right]$

